

# Sliding Mode Controller Based on the Sliding Mode Observer for a QBall 2+ Quadcopter with Experimental Validation

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## ABSTRACT

This paper studies a particular Unmanned Aerial Vehicle (UAV), called QBall 2+ quadcopter. This vehicle is a complex system, non-linear, strongly coupled, and under-actuated. First, a non-linear model was developed to represent the dynamics of the studied drone. Once the latter is established, the linear model was used to obtain the best gains of the Proportional Integral Derivative (PID) controller. This controller was applied after on the non-linear model of the UAV. Moreover, a Sliding Mode Controller (SMC) based on Sliding Mode Observer (SMO) was designed for retrieving the system unknown variables. Through these latter, the QBall 2+ was controlled, taking into account the observer errors. The first contribution in this work is to implement the PID regulator on the QBall 2+ flight controller to validate the results obtained by simulation. Secondly, due to the limitations of the Flex 3 cameras, especially when the drone is outside their working environment, the sliding mode observer was implemented to replace the cameras in order to measure the states of the system considered in this work. Simulation results of the different applied controllers were displayed to evaluate their effectiveness.

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## 1. Introduction

Recently, in the field of flying robots, the use of quadrotors has drastically increased. They have many advantages compared to the fixed-wing drones in terms of maneuverability, structure and versatility. Moreover, they have a simple mechanical design, a small size and a low cost [1, 2, 3, 4, 5, 6, 7]. Quadrotors are widely exploited in military and civilian missions such as, search and rescue, mapping, protection of sensitive points, and infrastructure inspection [8, 9, 10, 11, 12]. The QBall 2 quadcopter is an innovative platform intended for scientific research to fly indoor using Optitrack Flex-3 cameras [13]. It has a strongly coupled dynamics and an external protective cage [13, 14, 15, 16, 17]. It was built by Quanser, a Canadian robot manufacturing company. It has an open architecture design that allows operators to test a variety of controllers ranging from basic flight dynamics stabilizers to advanced multi-vehicle path planning and navigation algorithms. The drone has an on-board data acquisition system, an on-board computer and a suite of sensors. The Qball 2+ is an innovative rotary wing vehicle platform suitable for a wide variety of research applications on UAVs. However, it has a working environment limitation by the field of view of the Flex 3 cameras, which are sensitive to light resources and ground reflection. It is designed with an outer protective cage. In the real prototype, the cage gives the QBall 2+ a decisive advantage over other vehicles that would cause significant damage

in the event of contact between the vehicle and an obstacle, or in the event of a failure [13].

The researchers in paper [18], have performed an Extended Kalman Filter (EKF), this non-linear observer was exploited to control the QBall 2 drone. In addition, they have also applied a Linear Quadratic Regulator (LQR) on the same system to evaluate its performance. Moreover, the obtained results of the designed observer are satisfactory in the presence of model uncertainty. The authors in work [19], have designed an optimal PID controller with a Kalman filter. The latter is based on the time integral taking into account the errors of the system. However, they did not consider the different faults of the drone. In the same context, an Observer based on Sliding Mode Control (OSMC) has been considered in [20, 21, 22], to overcome the practical limitations of rotational and translation speed. A nonlinear PID controller with gains tuning has been implemented to follow the desired 3D trajectory of the QBall 2 quadrotor [23]. In addition, the experimental tests were carried out, where the quadrotor is subjected to external disturbances (gust of wind) in flight. An optimal fault tolerant controller was applied to stabilize the QBall 2 drone [24]. This approach is based mainly on a Finite Time Sliding Mode Observer (FTSMO), which estimates the completeness from outputs and allows to identify the disturbances type. In addition, the proposed strategy has proven its robustness under the influence of external disturbances and uncertainties. In reference [25], the researchers have introduced a new Lyapunov-based trajectory tracking approach to control and stabilize a quadrotor UAV. Furthermore, they have diagnosed an actuator failure using an intelligent output estimator. In article [26], two control algorithms have been applied on a quadrotor drone. The first one is designed to detect and diagnose actuator faults, where the second one works online after detecting the actuator faults. Kose et al. [27], have developed a dynamic model and Matlab simulation for the QBall 2. The developed model was validated through various flight scenarios. More recently, Wang et al. [28], have designed and applied an adaptive fault tolerant approach to control a small quadcopter. This approach was tested against actuator faults as well as unknown system parameters. However, the different external disturbances were not studied in this work.

The first contribution in this work is to implement the PID regulator on the QBall 2+ flight controller to validate the results obtained by simulation. To achieve this goal, the various "Optitrack Flex-3" cameras must be calibrated and tested to locate the position of the quadcopter. Secondly, due to the limitations of the Flex 3 cameras, especially when the drone is outside their working environment, the sliding mode observer was implemented to replace the cameras in order to measure the states of the system considered in this work.

The paper is structured as follows: In Section 1, a mathematical model that represents the dynamic behavior of the QBall 2 was developed. Section 2 explains the design steps of the different control techniques. Simulation results were displayed in Section 3. Section 4 is devoted to validate the PID controller through some experimental tests. Section 5 is intended for conclusion and future works.

## 2. Modeling of QBall 2+

The following assumptions are taken into account for the dynamic model of QBall 2+ [28]:

- The structure of the QBall 2+ is assumed to be rigid and symmetrical, which means that the inertia matrix is diagonal.
- The propellers are supposed to be rigid in order to neglect the effect of their deformation during the rotation.
- The inertia matrix  $J \in \mathbb{R}^{3 \times 3}$  is assumed to be constant.
- The origin of the body frame is supposed to coincide with the center of gravity (see Fig. 1).

With aim to simplify the understanding of the multitude of variables and terms of this work, the notation Table is given as follows (see Table 1).

**Table 1.** Table of notation.

Symbols	Notation
$[x \ y \ z]^T$	Position vector
$\dot{\chi} = [\dot{x} \ \dot{y} \ \dot{z}]^T$	Translation speeds vector.
$[\ddot{x} \ \ddot{y} \ \ddot{z}]^T$	Translation accelerations vector.
$[\theta \ \phi \ \psi]^T$	Euler angles vector.
$\Omega = [p \ q \ r]^T$	Rotation speed vector.
$\dot{\Omega} = [\dot{p} \ \dot{q} \ \dot{r}]^T$	Vector of angular accelerations.
$V = [u \ v \ \omega]^T$	Vector of linear velocities in the body frame.
$J$	Matrix of angular moments.
$I_{xx}$	Moment of inertia of the quadcopter along the x axis (Roll axes).
$I_{yy}$	Moment of inertia of the quadcopter along the y axis (Pitch axes).
$I_{yz}$	Moment of inertia of the quadcopter along the z axis (Yaw axes).
$J_r$	Represents the inertia matrix of each rotor.
$J_{rx}$	Inertia of the rotor along the x axis.
$J_{ry}$	Inertia of the rotor along the y axis.
$J_{rz}$	Inertia of the rotor along the z axis.
$M$	Mass of QBall 2+.
$P$	Weight of the QBall 2+.
$R_0$	Terrestrial landmark.
$R_1$	Landmark linked to the body of the quadcopter.
$R_p$	Crossing matrix of $R_0$ to $R_1$ .
$F_{gR_0}$	Force of gravity.
$F_i$	Thrust generated by each propeller.
$F_{PR_1}$	Lift created by the propellers in body frame.
$D_{R_1}$	Drag Force.
$K_d$	Drag coefficient.
$\tau_{R_1}$	Torques applied to the quadcopter.
$L$	Distance between the center of gravity and the axis of rotation of the rotor.
$\tau_i$	Torque generated by each motor.
$\tau_{gyr}$	Gyroscopic moment.
$K_v$	Voltage transformation constant at the input of each motor to angular velocity.
$v$	Battery output voltage.
$\tau_f$	Friction torque.
$k_f$	Coefficient of friction.
$U = [U_1 \ U_2 \ U_3 \ U_4]^T$	Control vector.
$u_i$	Input Pulse Width Modulation (PWM) of actuator $i$ .
$V_i$	Lyapunov's function.

## 2.1. Translation Dynamics

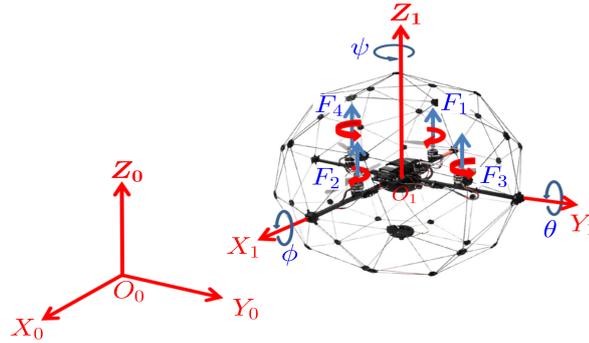
Using Newton-Euler's law, which is the sum of all external forces acting on a rigid body and equal the modulus of its mass per acceleration as following

$$\begin{aligned} F_{R_0} &= M \frac{d}{dt}(V_{R_0}) \\ F_{R_1} &= M V_{R_1} + M(\Omega \wedge V_{R_1}) \end{aligned} \quad (1)$$

where

$$\Omega \wedge V_{R_1} = \begin{bmatrix} qw - rv \\ ru - pw \\ pv - qu \end{bmatrix} \quad (2)$$

where  $(\Omega \wedge V_{R_1})$  is called the Coriolis term indicating the coriolis effects, and  $M$  is the quadrotor mass.



**Fig. 1.** Frames used to describe the movement of the Qball 2+.

The main forces applied on QBall 2+ are defined as

- **Force of gravity**

The force of gravity  $F_{g_{R_0}} = [0 \ 0 \ -Mg]^T$  in the fixed frame is along the  $Z$  axis (yaw axis), its expression in the mobile frame  $R_1$  is giving as follows

$$F_{g_{R_1}} = R_p^T F_{g_{R_0}} = R_p^T \begin{bmatrix} 0 \\ 0 \\ -Mg \end{bmatrix} = \begin{bmatrix} Mg \sin(\theta) \\ -Mg \sin(\phi) \cos(\theta) \\ -Mg \cos(\phi) \cos(\theta) \end{bmatrix} \quad (3)$$

with  $R_p^T$  is the passage matrix from the fixed frame to the body frame, and

$$R_p = \begin{bmatrix} C(\psi)C(\theta) & C(\psi)S(\theta)S(\phi) - S(\psi)C(\phi) & C(\psi)S(\theta)C(\phi) + S(\psi)S(\phi) \\ S(\psi)C(\theta) & S(\psi)S(\theta)S(\phi) + C(\psi)C(\phi) & S(\psi)S(\theta)C(\phi) - C(\psi)S(\phi) \\ -S(\theta) & C(\theta)S(\phi) & C(\theta)C(\phi) \end{bmatrix} \quad (4)$$

with

$$C(x) = \cos(x) \text{ and } S(x) = \sin(x).$$

- **Force of thrust**

It is a resultant obtained by the rotation of each rotor, it is parallel to the  $Z$  axis expressed in the body frame  $R_1$ . The thrust generated by each propeller is modeled using a first order function [13]. Its model is different to the model of the conventional quadrotors, where it is given by

$$F_i = K \frac{w}{s + w} u_i, \quad i = 1, 2, 3, 4. \quad (5)$$

with  $K$  is a positive gain and  $\omega$  is the actuator bandwidth.

- **Force of drag**

It's expressed in the body frame as [29, 30]

$$D_{R_1} = -K_d \dot{\chi} \quad (6)$$

with  $K_d$  represents the drag coefficient.

According to Equations (5) and (6), we get the various forces expressed in the body frame as following

$$F_{T_{R_1}} = F_{g_{R_1}} + F_P + D_{R_1} \quad (7)$$

Therefore, Equations (1) and (7) become

$$\begin{cases} M\dot{u} + M(qw - rv) = -Mg \sin(\theta) - K_x \dot{x} \\ M\dot{v} + M(ru - pw) = Mg \sin(\phi) \cos(\theta) - K_y \dot{y} \\ M\dot{w} + M(pv - qu) = Mg \cos(\theta) \cos(\psi) - K_z \dot{z} + F_{P_{R_1}} \end{cases} \quad (8)$$

## 2.2. Rotation Dynamics

Using Newton's second law, which is the sum of the external moments equal to the temporal variation of the angular momentum as follows

$$\begin{aligned} \tau_{R_0} &= J \frac{d}{dt} (\Omega_{R_0}) \\ \tau_{R_1} &= J\dot{\Omega} + \Omega \wedge J\Omega \end{aligned} \quad (9)$$

where  $\tau_{R_0}$  and  $\tau_{R_1}$  are the moments applied on the quadrotor expressed in the fixed and mobile frames respectively.

The different moments (roll, pitch, yaw), which cause the rotation of the QBall 2 along the three axes (see Fig. 2) are given as follows

$$\begin{cases} \tau_{\theta_{R_1}} = L(F_1 - F_2) \\ \tau_{\phi_{R_1}} = L(F_3 - F_4) \\ \tau_{\psi_{R_1}} = \tau_1 + \tau_2 - \tau_3 - \tau_4 \end{cases} \quad (10)$$

where  $L$  represents the distance between the center of gravity and the axis of rotation of the rotor,  $\tau_i$  is the torque generated by each rotor, it is assumed to have the following relation with respect to the PWM input as

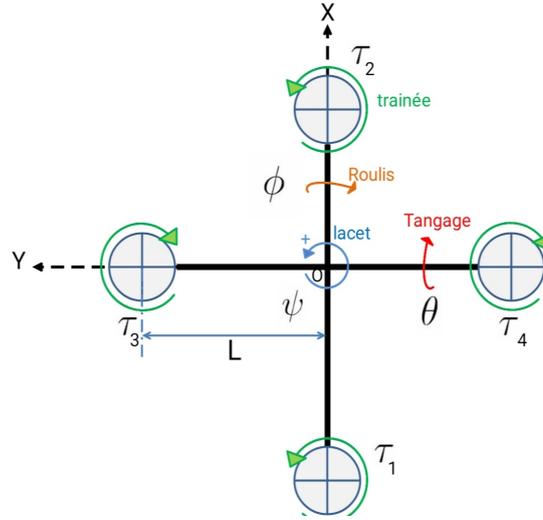
$$\tau_i = K_y u_i, \quad i = 1, 2, 3, 4. \quad (11)$$

where  $K_y$  is a positive gain.

- **Gyroscopic moment**

Its general expression is given by:

$$\tau_{gyr} = \begin{bmatrix} (u_3 + u_4 - u_1 - u_2) J_{rz} q K_v v \\ (u_1 + u_2 - u_3 - u_4) J_{rz} p K_v v \\ 0 \end{bmatrix} \quad (12)$$



**Fig. 2.** Schematic representation of QBall 2+.

### • Friction torque

It's the resultant of the aerodynamic friction couples. It is modeled as

$$\tau_f = k_f \Omega^2 \quad (13)$$

with

$$k_f = \begin{bmatrix} k_{fx} & 0 & 0 \\ 0 & k_{fy} & 0 \\ 0 & 0 & k_{fz} \end{bmatrix} \quad (14)$$

Equation (9) becomes

$$\begin{cases} J_{xx}\dot{p} + qr(J_{zz} - J_{yy}) = L(F_3 - F_4) - J_{rz}qu_g - k_{fx}p^2 \\ J_{yy}\dot{q} + pr(J_{xx} - J_{zz}) = L(F_1 - F_2) + J_{rz}pu_g - k_{fy}q^2 \\ J_{zz}\dot{r} + pq(J_{yy} - J_{xx}) = \tau_1 + \tau_2 - \tau_3 - \tau_4 - k_{fz}r^2 \end{cases} \quad (15)$$

with  $u_g = (u_1 + u_2 - u_3 - u_4)K_v v$ .

Due to the weak orientations of QBall 2+, the relation which connects the angular speeds expressed in reference  $R_1$  and the derivatives of the angles of Euler expressed in reference  $R_0$  is given by

$$(\dot{\phi}, \dot{\theta}, \dot{\psi}) \approx (p, q, r) \quad (16)$$

From Equations (8), (15) and (16), the dynamics model of QBall 2+ in the fixed frame is represented by the following state equations

$$\begin{cases} \ddot{x} = \frac{1}{M} F_{PR_1} (C(\psi)S(\theta)C(\phi) + S(\psi)S(\phi)) - \frac{K_x}{M} \dot{x} \\ \ddot{y} = \frac{1}{M} F_{PR_1} (S(\psi)S(\theta)C(\phi) - C(\psi)S(\phi)) - \frac{K_y}{M} \dot{y} \\ \ddot{z} = \frac{1}{M} F_{PR_1} (C(\theta)C(\phi)) - \frac{K_z}{M} \dot{z} - g \\ \ddot{\phi} = \frac{L(F_3 - F_4)}{J_{xx}} - \frac{J_{rz}qu_g}{J_{xx}} - \frac{\dot{\theta}\dot{\psi}(J_{zz} - J_{yy})}{J_{xx}} - \frac{k_{fx}}{J_{xx}} p^2 \\ \ddot{\theta} = \frac{L(F_1 - F_2)}{J_{yy}} + \frac{J_{rz}pu_g}{J_{yy}} - \frac{\dot{\phi}\dot{\psi}(J_{xx} - J_{zz})}{J_{yy}} - \frac{k_{fy}}{J_{yy}} q^2 \\ \ddot{\psi} = \frac{\tau_1 + \tau_2 - \tau_3 - \tau_4}{J_{zz}} - \frac{\dot{\phi}\dot{\theta}(J_{yy} - J_{xx})}{J_{zz}} - \frac{k_{fz}}{J_{zz}} r^2 \end{cases} \quad (17)$$

### 3. Control of QBall 2+

#### 3.1. Linear Control Model

In the almost stationary state, it is shown that the total thrust is approximately equal to the weight, i.e.  $F_{P_{R1}} \approx Mg$  [31]. Due to the small amplitude movements of QBall 2+, it's assumed that

$$\cos(\phi) = 1; \cos(\theta) = 1; \cos(\psi) = 1 \text{ and } \sin(\phi) = \phi; \sin(\theta) = \theta; \sin(\psi) = \psi \quad (18)$$

Then, the dynamics of QBall 2 expressed by Equation (17) can be simplified as follows:

$$\begin{cases} \ddot{x} = g\theta \\ \ddot{y} = -g\phi \\ \ddot{z} = \frac{1}{M}F_{P_{R1}} - g \\ \ddot{\phi} = \frac{L(F_3 - F_4)}{J_{xx}} \\ \ddot{\theta} = \frac{L(F_1 - F_2)}{J_{yy}} \\ \ddot{\psi} = \frac{\tau_1 + \tau_2 - \tau_3 - \tau_4}{J_{zz}} \end{cases} \quad (19)$$

#### 3.2. Nonlinear Control Model

For the nonlinear control model, the state equations are used as

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = a_1x_4x_6 + a_2x_2^2 + a_3x_4u_g + b_1U_2 \\ \dot{x}_3 = x_4 \\ \dot{x}_4 = a_4x_2x_6 + a_5x_4^2 + a_6x_2u_g + b_2U_3 \\ \dot{x}_5 = x_6 \\ \dot{x}_6 = a_7x_2x_4 + a_8x_6^2 + b_3U_4 \\ \dot{x}_7 = x_8 \\ \dot{x}_8 = a_9x_8 + \frac{U_x}{M}U_1 \\ \dot{x}_9 = x_{10} \\ \dot{x}_{10} = a_{10}x_{10} + \frac{u_y}{M}U_1 \\ \dot{x}_{11} = x_{12} \\ \dot{x}_{12} = a_{11}x_{12} + \frac{1}{M}U_1c(x_1)c(x_3) - g \end{cases} \quad (20)$$

with

$$a_1 = -\frac{(J_{zz} - J_{yy})}{J_{xx}}, a_2 = -\frac{k_{fx}}{J_{xx}}, a_3 = -\frac{J_{rx}}{J_{xx}}, b_1 = \frac{L}{J_{xx}}$$

$$a_4 = -\frac{(J_{xx} - J_{zz})}{J_{yy}}, a_5 = -\frac{k_{fy}}{J_{yy}}, a_6 = \frac{J_{ry}}{J_{yy}}, b_2 = \frac{L}{J_{yy}}$$

$$a_7 = -\frac{(J_{yy}-J_{xx})}{J_{zz}}, a_8 = -\frac{k_{fz}}{J_{zz}}, b_3 = \frac{1}{J_{zz}}$$

$$a_9 = -\frac{K_x}{M}, a_{10} = -\frac{K_y}{M}, a_{11} = -\frac{K_z}{M}$$

$$U_X = C(x_1)S(x_3)C(x_5) + S(x_1)S(x_5)$$

$$U_y = C(x_1)S(x_3)S(x_5) - S(x_1)C(x_5)$$

The control vector is expressed by a thrust force and moments as

$$U = [U_1 \ U_2 \ U_3 \ U_4]^T$$

with

$$\begin{bmatrix} U_1 \\ U_2 \\ U_3 \\ U_4 \end{bmatrix} = \begin{bmatrix} k & k & k & k \\ 0 & 0 & k & -k \\ k & -k & 0 & 0 \\ k_y & k_y & -k_y & -k_y \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \end{bmatrix} \quad (21)$$

The choice of state vector is given as follows

$$X = \left\{ \phi \ \dot{\phi} \ \theta \ \dot{\theta} \ \psi \ \dot{\psi} \ x \ \dot{x} \ y \ \dot{y} \ z \ \dot{z} \right\} \quad (22)$$

The system outputs are given as

$$Y = [\phi \ \theta \ \psi \ x \ y \ z]^T$$

### 3.3. PID Controller Design

Here, the PID controller based on the linear model presented by (19) is designed. This control law will be applied after to the nonlinear control model presented by (20).

The PID control laws are given as

$$U_1 = K_{pz}e_z + K_{iz} \int_0^{+\infty} e_z + K_{dz} \frac{de_z}{dt} \quad (23)$$

$$U_2 = K_{p\phi}e_\phi + K_{i\phi} \int_0^{+\infty} e_\phi + K_{d\phi} \frac{de_\phi}{dt} \quad (24)$$

$$U_3 = K_{p\theta}e_\theta + K_{i\theta} \int_0^{+\infty} e_\theta + K_{d\theta} \frac{de_\theta}{dt} \quad (25)$$

$$U_4 = K_{p\psi}e_\psi + K_{i\psi} \int_0^{+\infty} e_\psi + K_{d\psi} \frac{de_\psi}{dt} \quad (26)$$

After choosing the altitude and attitude regulators, a position controller is developed. The PID controllers are used to calculate the desired positions [32], and the desired roll  $\phi_d$  and pitch  $\theta_d$  angles, which are given by

$$\begin{cases} \theta_d = K_{px} * e_x + K_{ix} * \int_0^{+\infty} e_x + K_{dx} * \frac{de_x}{dt} \\ \phi_d = K_{py} * e_y + K_{iy} * \int_0^{+\infty} e_y + K_{dy} * \frac{de_y}{dt} \end{cases} \quad (27)$$

with  $e_z = z_d - z$ ,  $e_\phi = \phi_d - \phi$ ,  $e_\theta = \theta_d - \theta$ ,  $e_\psi = \psi_d - \psi$ ,  $e_x = x_d - x$ ,  $e_y = y_d - y$ , and  $K_P$ ,  $K_i$  and  $K_d$  are respectively proportional, integral and derivative gains.

### 3.4. Sliding Mode Observer (SMO) Design

#### 3.4.1 Sliding Mode Observer State Model

In this subsection, a nonlinear sliding mode observer is designed. The latter will be tested against uncertain system parameters. The observer state model is given by

$$\hat{\Sigma} : \begin{cases} \hat{x}_1 = \hat{x}_2 + \Lambda_1(z_1) \\ \hat{x}_2 = a_1 \hat{x}_4 \hat{x}_6 + a_2 \hat{x}_2^2 + a_3 \hat{x}_4 u_g + b_1 U_2 + \Lambda_2(z_2) \\ \hat{x}_3 = \hat{x}_4 + \Lambda_3(z_3) \\ \hat{x}_4 = a_4 \hat{x}_2 \hat{x}_6 + a_5 \hat{x}_4^2 + a_6 \hat{x}_2 u_g + b_2 U_3 + \Lambda_4(z_4) \\ \hat{x}_5 = \hat{x}_6 + \Lambda_5(z_5) \\ \hat{x}_6 = a_7 \hat{x}_2 \hat{x}_4 + a_8 \hat{x}_6^2 + b_3 U_4 + \Lambda_6(z_6) \\ \hat{x}_7 = \hat{x}_8 + \Lambda_7(z_7) \\ \hat{x}_8 = a_9 \hat{x}_8 + \frac{\hat{U}_x}{M} U_1 + \Lambda_8(z_8) \\ \hat{x}_9 = \hat{x}_{10} + \Lambda_9(z_9) \\ \hat{x}_{10} = a_{10} \hat{x}_{10} + \frac{\hat{U}_y}{M} U_1 + \Lambda_{10}(z_{10}) \\ \hat{x}_{11} = \hat{x}_{12} + \Lambda_{11}(z_{11}) \\ \hat{x}_{12} = a_{11} \hat{x}_{12} + \frac{1}{M} U_1 (c(\hat{x}_1) c(\hat{x}_3)) - g + \Lambda_{12}(z_{12}) \end{cases} \quad (28)$$

where the dynamic of the observer errors is expressed as follows

$$\begin{cases} \dot{z}_1 = z_2 - \Lambda_1 \\ \dot{z}_2 = a_1 \Delta_{x_4 x_6} + a_2 \Delta_{x_2^2} + a_3 \Delta_{x_4} u_g - \Lambda_2 \\ \dot{z}_3 = z_4 - \Lambda_3 \\ \dot{z}_4 = a_4 \Delta_{x_2 x_6} + a_5 \Delta_{x_4^2} + a_6 \Delta_{x_2} u_g - \Lambda_4 \\ \dot{z}_5 = z_6 - \Lambda_5 \\ \dot{z}_6 = a_7 \Delta_{x_2 x_4} + a_8 \Delta_{x_6^2} - \Lambda_6 \\ \dot{z}_7 = z_8 - \Lambda_7 \\ \dot{z}_8 = a_9 z_8 + \frac{1}{M} \Delta_{U_x} U_1 - \Lambda_8 \\ \dot{z}_9 = z_{10} - \Lambda_9 \\ \dot{z}_{10} = a_{10} z_{10} + \frac{1}{M} \Delta_{U_y} U_1 - \Lambda_{10} \\ \dot{z}_{11} = z_{12} - \Lambda_{11} \\ \dot{z}_{12} = a_{11} z_{12} + \frac{1}{M} U_1 \Delta_{(c(x_1)c(x_3))} - \Lambda_{12} \end{cases} \quad (29)$$

with

$$\begin{cases} \Delta_{x_i x_j} = x_i x_j - \hat{x}_i \hat{x}_j & \Delta_{(c(x_1)c(x_3))} = (c(x_1)c(x_3)) - (c(\hat{x}_1)c(\hat{x}_3)) \\ \Delta_{x_i^2} = x_i^2 - \hat{x}_i^2 & \Delta_{U_x} = U_x - U_{\hat{x}} \\ \Delta_{x_i} = x_i - \hat{x}_i & \Delta_{U_y} = U_y - U_{\hat{y}} \end{cases} \quad (30)$$

and

$$\begin{cases} z_i = y_i - \hat{y}_i & \text{if } i \text{ odd.} \\ z_i = x_i - \hat{x}_i & \text{if } i \text{ pair.} \end{cases} \quad (31)$$

with

$$\Lambda_i(z_i) = K_i \text{sign}(x_i - \hat{x}_i)$$

### 3.4.2 Observer Design Assumptions

With the aim to design the sliding mode observer, we must define the measured states and the missing states. The measurements of the optitrack cameras are:

$$\begin{cases} \phi = x_1 & \dot{\phi} = x_2 & x = x_7 \\ \theta = x_3 & \dot{\theta} = x_4 & y = x_9 \\ \psi = x_5 & \dot{\psi} = x_6 & z = x_{11} \end{cases} \quad (32)$$

Nevertheless, the unmeasured states are given as

$$\begin{cases} \dot{x} = x_8 \\ \dot{y} = x_{10} \\ \dot{z} = x_{12} \end{cases} \quad (33)$$

### 3.4.3 Observer Stability Analysis

In order to study the stability and the convergence of the observer, it's necessary to choose the candidate Lyapunov function, which is a function of the error and then the stability has to be proved. The errors must converge to zero i.e. the estimated states must converge to the actual states after the following steps.

- **Step 1:** Considering the dynamics of the error of the first observer as

$$\dot{z}_1 = z_2 - K_1 \text{sign}(z_1) \quad (34)$$

The choose of the Lyapunov function is giving as following

$$V_1 = \frac{1}{2} z_1^2 \quad (35)$$

Its derivative is given as

$$\dot{V}_1 = z_1 \dot{z}_1 = z_1(z_2 - K_1 \text{sign}(z_1)) \quad (36)$$

So that  $\hat{x}_1 \rightarrow x_1$  it is necessary that  $\dot{V}_1 < 0$ . For that, the  $K_1$  is chosen as

$$K_1 > |z_2|_{max} \quad (37)$$

Then, the error  $z_1 \rightarrow 0$  after a finite time  $t_1$ , which gives

$$z_2 = K_1 \text{sign}(z_1) \quad (38)$$

After that,  $x_2$  becomes

$$x_2 = \hat{x}_2 + K_1 \text{sign}(z_1) \quad (39)$$

- **Step 2:** In this step,  $z_2$  converges towards zero.

To stay on the surface  $z_2 = 0$ , it must be  $K_1 > |z_2|_{max}$ , but this is verified if  $z_2$  decreases after  $t_1$ .

The dynamics of error  $z_2$  becomes

$$\dot{z}_2 = a_1 \Delta_{x_4 x_6} + a_2 \Delta_{x_2^2} + a_3 \Delta_{x_4} u_g - K_2 \text{sign}(z_2)$$

Then, the Lyapunov function is taken as

$$V_2 = \frac{1}{2} z_1^2 + \frac{1}{2} z_2^2$$

Its derivative is

$$\dot{V}_2 = z_1 \dot{z}_1 + z_2 \dot{z}_2 = z_2 (a_1 \Delta_{x_4 x_6} + a_2 \Delta_{x_2^2} + a_3 \Delta_{x_4} u_g - K_2 \text{sign}(z_2))$$

To get  $\dot{V}_2 < 0$ , it's necessary to choose

$$K_2 > |a_1 \Delta_{x_4 x_6} + a_2 \Delta_{x_2^2} + a_3 \Delta_{x_4} u_g|_{max}$$

Therefore,  $z_2 \rightarrow 0$  after a finite time  $t_2$ .

The steps 3, 5, 7, 9, and 11 are identical to step 1, where the obtained results are:

- **Step 3:**  $K_3 > |z_4|_{max}$ , therefore  $z_3 \rightarrow 0$  after a  $t_3$  finished, and  $x_4 = \hat{x}_4$ .
- **Step 5:**  $K_5 > |z_6|_{max}$ , therefore  $z_6 \rightarrow 0$  after a  $t_5$  finished, and  $x_6 = \hat{x}_6$ .
- **Step 7:**  $K_7 > |z_8|_{max}$ , therefore  $z_7 \rightarrow 0$  after a  $t_7$  finished, and  $x_8 = \hat{x}_8$ .
- **Step 9:**  $K_9 > |z_{10}|_{max}$ , therefore  $z_9 \rightarrow 0$  after a  $t_9$  finished, and  $x_{10} = \hat{x}_{10}$ .
- **Step 11:**  $K_{11} > |z_{12}|_{max}$ , therefore  $z_{11} \rightarrow 0$  after a  $t_{11}$  finished, and  $x_{12} = \hat{x}_{12}$ .

Also for the steps 4, 6, 8, 10, and 12 will be identical to step 2.

- **Step 4:** The dynamics of error  $z_4$  will be:

$$\dot{z}_4 = a_4 \Delta_{x_2 x_6} + a_5 \Delta_{x_4^2} - K_4 \text{sign}(z_4)$$

Involved

$$K_4 > |a_4 \Delta_{x_2 x_6} + a_5 \Delta_{x_4^2}|_{max}$$

To ensure the convergence of  $z_4 \rightarrow 0$  after a finite time  $t_4$ .

- **Step 6:** The dynamics of error  $z_6$  will be

$$\dot{z}_6 = a_8 \Delta_{x_6^2} - K_6 \text{sign}(z_6)$$

Involved

$$K_6 > |a_8 \Delta_{x_6^2}|_{max}$$

To ensure the convergence of  $z_6 \rightarrow 0$  after a finite time  $t_6$ .

- **Step 8:** The dynamics of error  $z_8$  will be

$$\dot{z}_8 = -K_8 \text{sign}(z_8)$$

$(U_x - U_{\hat{x}}) = 0$  because  $U_x$  and  $U_{\hat{x}}$  are modeled according to  $(x_1, x_3, x_5)$  and  $(\hat{x}_1, \hat{x}_3, \hat{x}_5)$  respectively.

Here, the choice of  $K_8$  is given as

$$K_8 > 0$$

To ensure the convergence of  $z_8 \rightarrow 0$  after a finite time  $t_8$ .

- **Step 10:** The dynamics of error  $z_{10}$  will be

$$\dot{z}_8 = -K_{10} \text{sign}(z_{10})$$

$(U_y - U_{\hat{y}}) = 0$  because  $U_y$  and  $U_{\hat{y}}$  are modeled according to  $(x_1, x_3, x_5)$  and  $(\hat{x}_1, \hat{x}_3, \hat{x}_5)$  respectively.

The choice of  $K_{10}$  is given as

$$K_{10} > 0$$

To ensure the convergence of  $z_{10} \rightarrow 0$  after a finite time  $t_{10}$ .

- **Step 12:** The dynamics of error  $z_{12}$  will be

$$\dot{z}_{12} = -K_{12} \text{sign}(z_{12})$$

$\Delta_{(c(x_1)c(x_3))} = 0$  are modelled according to  $(x_1, x_3)$  and  $(\hat{x}_1, \hat{x}_3)$ .

In this step, the choice of  $K_{12}$  is given as

$$K_{12} > 0$$

To ensure the convergence of  $z_{12} \rightarrow 0$  after a finite time  $t_{12}$ .

### 3.5. Sliding Mode Control Law Design

The choice of the sliding surface is given by a general form as

$$S = \dot{Z}_i + \alpha_i Z_i, \quad Z_i = x_{id} - x_i \quad (40)$$

Its derivative is obtained as

$$\dot{S}_i = -k_i \text{sign}(S_i) = \ddot{Z}_i + \alpha_i \dot{Z}_i \quad (41)$$

The control law  $U_1$  is developed as follows.

We assume that

$$z_{11} = z_d - x_{11} \implies \dot{z}_{11} = \dot{z}_d - \dot{x}_{11} = \dot{z}_d - x_{12} \quad (42)$$

We replace  $x_{12}$  by  $\hat{x}_{12} + e_{12}$

$$\ddot{z}_{11} = \ddot{z}_d - \dot{x}_{12} = \ddot{z}_d - (\dot{\hat{x}}_{12} + \dot{e}_{12}) \quad (43)$$

Therefore

$$\ddot{z}_{11} = \ddot{z}_d - e_{12} - g - k_{12} \text{sat}(e_{11}) - \frac{C(x_1)C(x_2)}{M} U_1 \quad (44)$$

Now, we suppose that  $e_{12}$  and  $\dot{e}_{12}$  are bounded which gives:

$$\begin{cases} e_{12} \leq |e_{12}|_{\max} = \beta_{12} e \\ \dot{e}_{12} \leq |\dot{e}_{12}|_{\max} = \dot{\beta}_{12}. \end{cases} \quad (45)$$

Thus

$$\dot{S}_{11} = g + \ddot{z}_d - \dot{e}_{12} - k_{12} \text{sat}(e_{11}) + \alpha_{11} (\dot{z}_d - \hat{x}_{12} - e_{12}) - \frac{C(x_1)C(x_2)}{M} U_1 - a_{11} \hat{x}_{12} = -k_{11} \text{sign}(S_{11}) \quad (46)$$

We use the upper terms, we find

$$U_1 = \frac{M}{C(x_1)C(x_2)} (k_{11} \text{sign}(S_{11}) + \alpha_{11} (\dot{z}_d - \hat{x}_{12} - \beta_{12}) + g + \ddot{z}_d - a_{11} \hat{x}_{12} - \dot{\beta}_{12} - K_{12} \text{sat}(e_{11})) \quad (47)$$

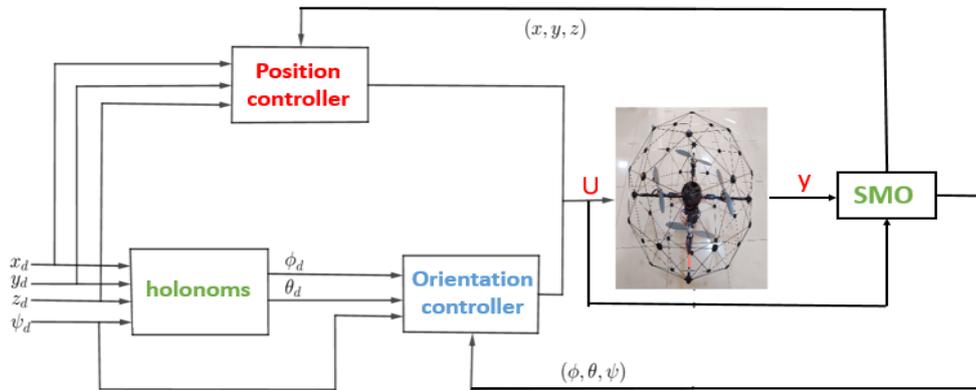
Adopting the same steps of development, we obtain the others controllers represented by the system of equations as

$$\begin{cases} U_2 = \frac{1}{b_1} [k_1 \text{sign}(S_\phi) + \ddot{\phi}_d + \alpha_1 (\dot{\phi}_d - x_2) - a_1 x_4 x_6 \\ \quad - a_2 x_2^2 - a_3 x_4 u_g] \\ U_3 = \frac{1}{b_2} [k_3 \text{sign}(S_\theta) + \ddot{\theta}_d + \alpha_3 (\dot{\theta}_d - x_4) - a_4 x_2 x_6 \\ \quad - a_5 x_4^2 - a_6 x_2 u_g] \\ U_4 = \frac{1}{b_3} [k_5 \text{sign}(S_\psi) + \ddot{\psi}_d + \alpha_5 (\dot{\psi}_d - x_6) - a_7 x_2 x_4 \\ \quad - a_8 x_6^2] \end{cases} \quad (48)$$

and

$$\begin{cases} U_x = \frac{M}{U_1} (k_7 \text{sign}(S_7) + \ddot{x}_d - a_9 \hat{x}_8 - K_8 \text{sat}(e_7) - \dot{\beta}_8 + \alpha_7 (\dot{x}_d - \hat{x}_8 - \beta_8)) \\ U_y = \frac{M}{U_1} (k_9 \text{sign}(S_9) + \ddot{y}_d - a_{10} \hat{x}_{10} - K_{10} \text{sat}(e_9) - \dot{\beta}_{10} + \alpha_9 (\dot{y}_d - \hat{x}_{10} - \beta_{10})) \end{cases} \quad (49)$$

Fig. 3 shows the block diagram of the sliding mode observer developed in this work.



**Fig. 3.** Block diagram of the sliding mode observer.

The Qball 2+ control architecture is composed of three main blocks, the position control block to control the translations  $(x, y, z)$ , the orientation control block to control the attitude  $(\varphi, \theta, \psi)$  and the sliding mode observer block (see Fig. 3). The latter is used in order to replace the Flex 3 cameras when the drone is outside the working environment of the cameras. In this case, the states of the system are not measurable and the control of the drone will be lost.

#### 4. Simulation Results

Before displayed the obtained results, the parameters of Qball 2+ are presented in Table 2. The PID and SMO observer parameters are given in Table 3, Table 4 and Table 5 respectively. Fig. 4, Fig. 5, Fig. 6, and Fig. 7 show the simulation results of the PID controller. Fig. 8, Fig. 9 and Fig. 10 show the simulation results of the SMO.

**Table 2.** QBall 2+ parameters.

Parameter	Definition	Value	Unit
$K_t$	Lift coefficient	12	N
$K_d$	Drag coefficient	0.4	N.m
$K_v$	Transformation constant	106.8	rad.s $V^{-1}$
$M$	Mass	1.79	Kg
$L$	Distance between the center of gravity and the center of each rotor	0.2	m
$I_x$	Moment of inertia of QBall 2 with respect to X axis	0.03	$Kg.m^2$
$I_y$	Moment of inertia of QBall 2 with respect to Y axis	0.03	$Kg.m^2$
$I_z$	Moment of inertia of QBall 2 with respect to Z axis	0.04	$Kg.m^2$
$J_{rz}$	Moment of inertia of rotor with respect to Z axis	0.0018	$Kg.m^2$
$\omega$	Actuator bandwidth	15	rad/s
$V_{max}$	Maximum input voltage	12	V

##### 4.1. Result and Discussion

Fig. 4 and Fig. 5 show that the evolution curves of the positions  $x$ ,  $y$  and  $z$  follow the desired states with some errors. These latter appear when the quadrotor changes its positions. For the attitude dynamics, it's observed from Fig. 5 and Fig. 6 that, the Euler angles  $(\phi, \theta, \psi)$  follow the reference angles with less accuracy compared to the positions  $(x, y, z)$ . The control signals displayed in Fig. 7 vary according to the change of their corresponding positions (see Fig. 5). Overall, the results obtained by the PID controller are acceptable.

**Table 3.** PID controller parameters used in simulations.

z	$K_{pz} = 0.5, K_{iz} = 0.02, K_{dz} = 0.15$	$\phi$	$K_{p\phi} = 2, K_{i\phi} = 0, K_{d\phi} = 0.3$
x	$K_{px} = 0.5, K_{ix} = 0, K_{dx} = 0.4$	$\theta$	$K_{p\theta} = 2, K_{i\theta} = 0, K_{d\theta} = 0.3$
y	$K_{py} = 0.5, K_{iy} = 0, K_{dy} = 0.4$	$\psi$	$K_{p\psi} = 0.45, K_{i\psi} = 0, K_{d\psi} = 0.3$

**Table 4.** SMO parameters used in simulations.

$k_1$	$k_3$	$k_5$	$k_7$	$k_9$	$k_{11}$	$\beta_8$	$\beta_{10}$	$\beta_{12}$	$\dot{\beta}_8$	$\dot{\beta}_{10}$	$\dot{\beta}_{12}$
5	5	4.5	9	9	15	0.3	0.35	0.9	1.4	1.2	1.3
$\alpha_1$	$\alpha_3$	$\alpha_5$	$\alpha_7$	$\alpha_9$	$\alpha_{11}$	$K_8$	$K_{10}$	$K_{12}$			
6	7	7	5	5	12	1	1.5	1.3			

**Table 5.** Observer gains.

Parameter	K1	K2	K3	K4	K5	K6	K7	K8	K9	K10	K11	K12
Values	15	17	10	13	12	16.5	14	15	11	13	14.5	17

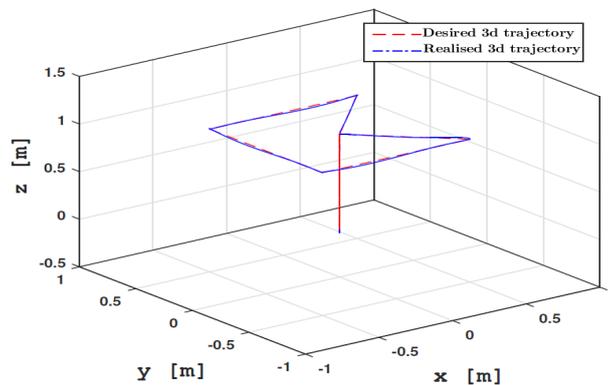
**Fig. 4.** Evolution of 3D trajectory for the PID controller.

Fig. 8 and Fig. 9 display the evolution of the desired trajectory, realized trajectory and the observed trajectory of the Qball 2+. It's clear that the trajectory realized by the QBall 2+ follows the reference trajectory with some tracking errors in the beginning (see Fig. 8 and Fig. 9). It can be concluded that the observed states converge rapidly towards the desired states in a finite time, whether for the positions or the Euler angles. Fig. 10 shows the evolution of the control signals. The controller  $U_1$  starts from a maximum value and then stabilizes around a constant value. It is clear that the evolution of  $U_2, U_3$  and  $U_4$  depends on the evolution of the translation and the rotation of the quadrotor (see Fig. 10). The obtained results (see Fig. 8, Fig. 9 and Fig. 10), have shown that the sliding mode observer has proven its efficiency against uncertain parameters of the system.

#### 4.2. Comparative Study

In this section, a comparative study between two control laws simulated previously (PID and SMO) will be carried out. With the aim to facilitate the comparison between the applied control laws,

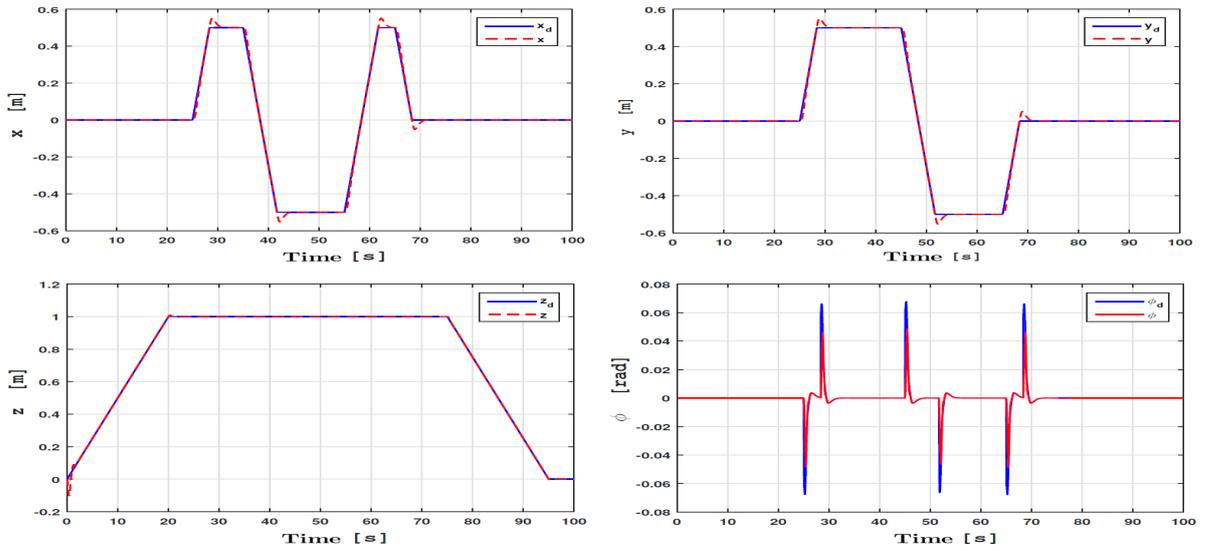


Fig. 5. Evolution of positions and roll angles for the PID controller.

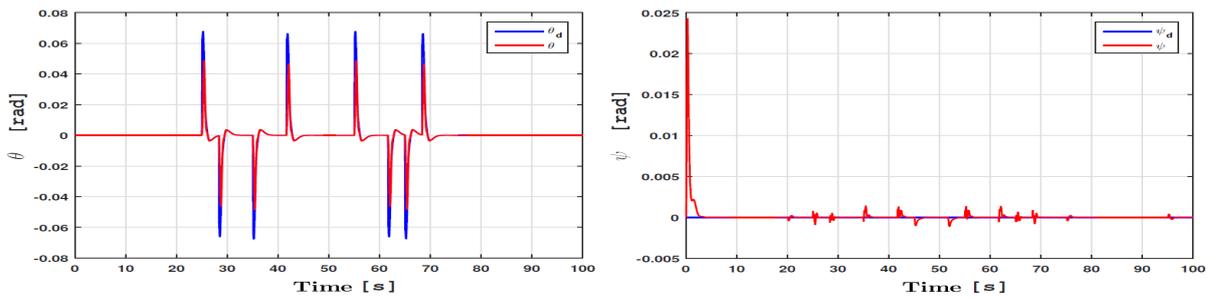


Fig. 6. Evolution of pitch and yaw angles for the PID controller.

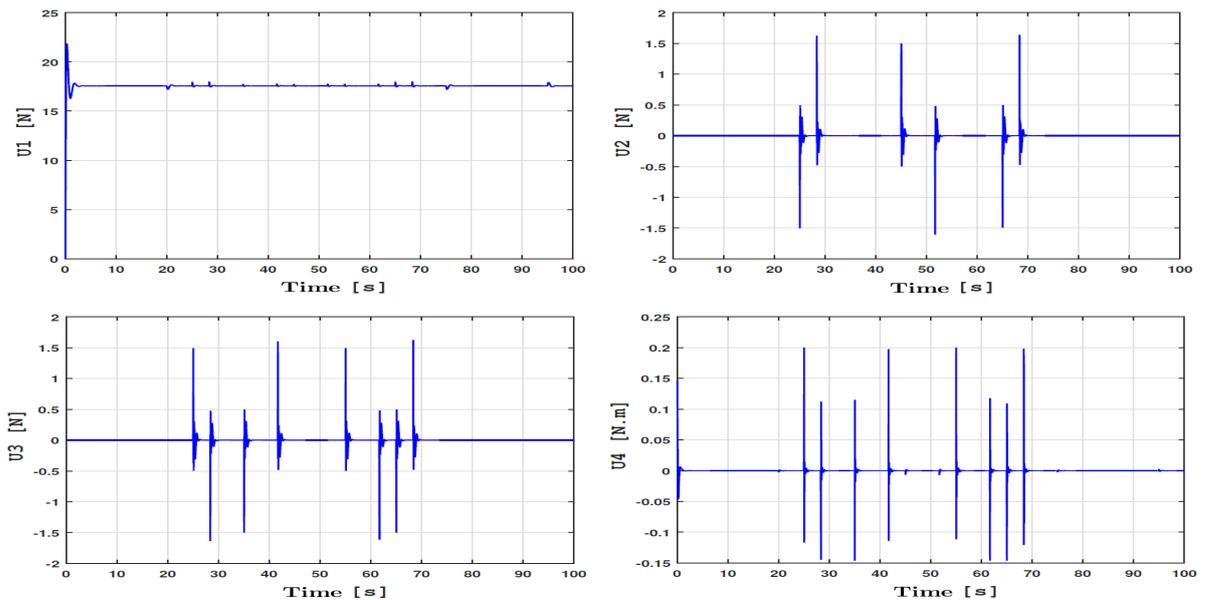


Fig. 7. Input signals for the PID controller.

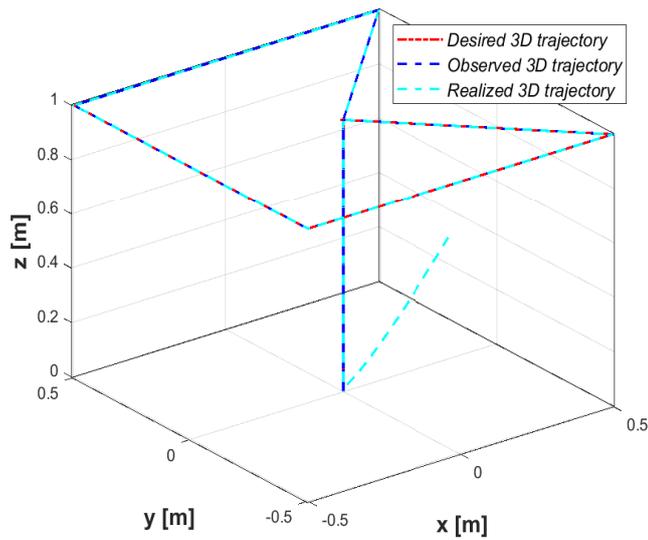


Fig. 8. Evolution of 3D trajectory for SMO.

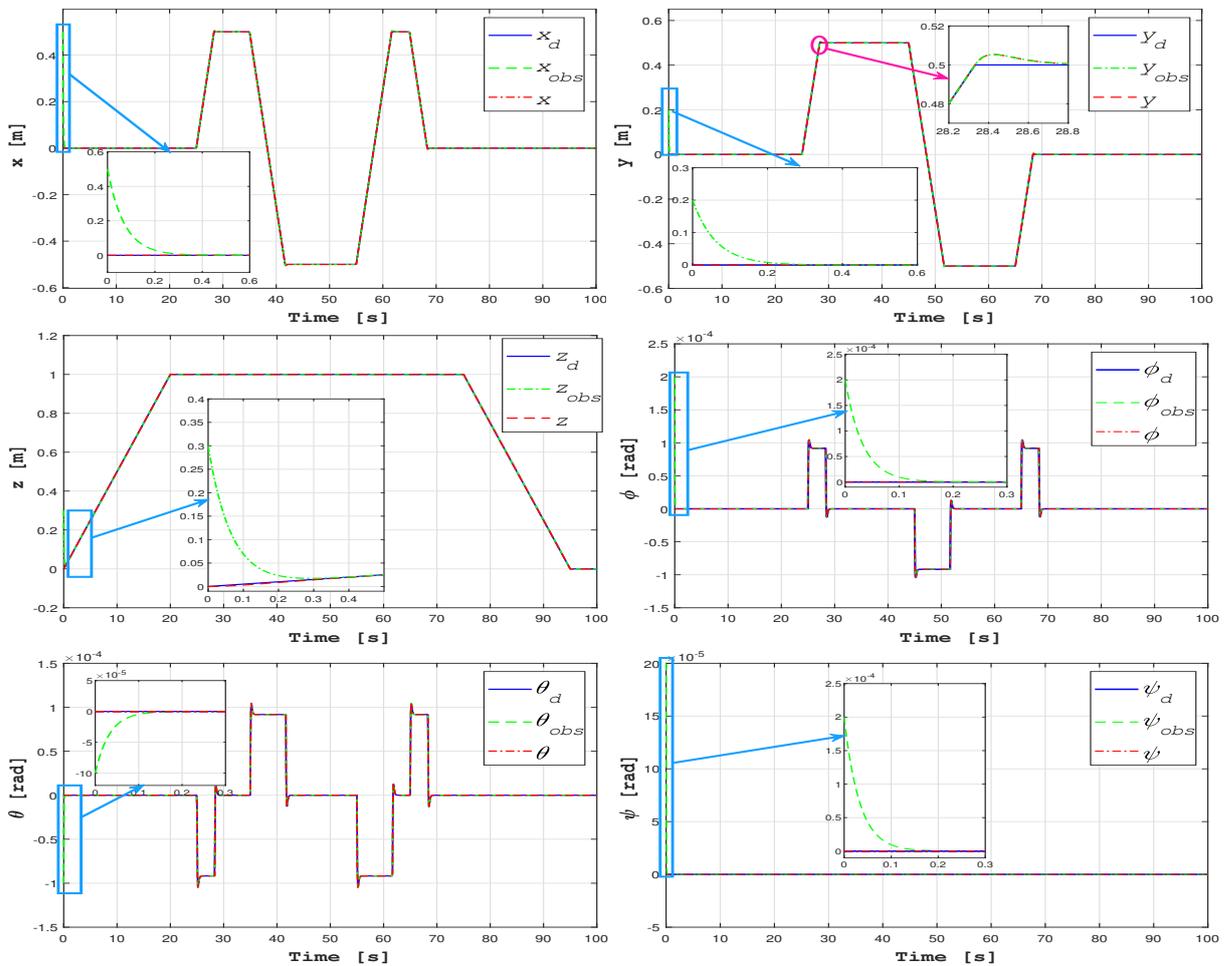
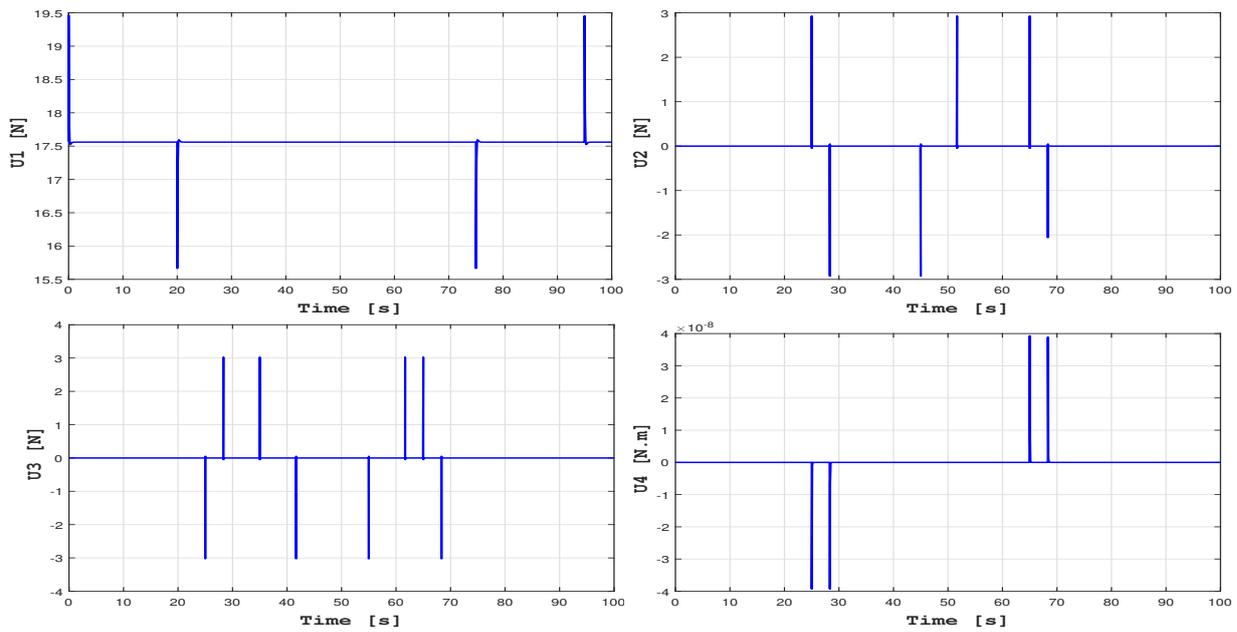


Fig. 9. Evolution of positions and Euler angles for the SMO.

two criteria will be adopted as follows:

$$J(e) = \frac{1}{k} \sum_{i=1}^k (e_x^2 + e_y^2 + e_z^2 + e_\theta^2 + e_\phi^2 + e_\psi^2)$$



**Fig. 10.** Input signals for the SMO.

$$J(u) = \frac{1}{k} \sum_{i=1}^k (u_1^2 + u_2^2 + u_3^2 + u_\theta^2 + u_x^2 + u_y^2)$$

where  $J(e)$  represents the quadratic tracking error,  $J(u)$  represents the energy and  $k$  is the number of samples.

**4.2.1 Results Interpretation**

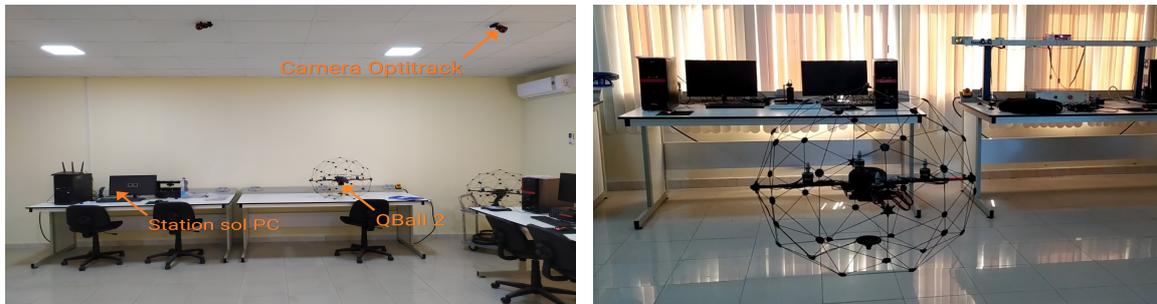
In this part, the energies of the control signals and their quadratic errors in a simulation time of 100s and a sampling step  $10^{-3}s$  will be calculated. According to the criteria of the squared errors and energies (see Table 6), it can be observed that, the SMO has proven its effectiveness in terms of accuracy and consumed energy compared to the results obtained by the conventional PID. Unlike the obtained results in works [33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44], where the initial conditions are zero, the SMO has presented good performance.

**Table 6.** Energies and quadratic errors of the controllers

	PID		SMO	
	J(e)	J(u)	J(e)	J(u)
	$20.41823 \cdot 10^{-6}$	$3.0852 \cdot 10^2$	$7.280 \cdot 10^{-6}$	$3.0836 \cdot 10^2$

## 5. Experimental validation

In this Section, a PID controller will be implemented in the control flight of QBall 2+ with the same parameters that we have used in simulation. Before launching the flight scenario, the different cameras "Optitrack Flex-3" must be calibrated and tested to locate the drone position as shown in Fig. 13, Fig. 14, Fig. 15 and Fig. 16.



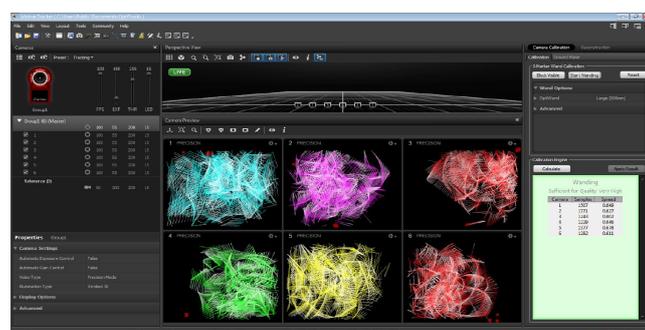
**Fig. 11.** To the left, QBall 2+ equipments. To the right, QBall 2+ in flight tests.

### 5.1. Cameras Flex-3 calibration steps

1. Launching the motivates software to determine the limits of the field of view.
2. Checking if there are no stray objects in the field of vision.
3. Definition of the origin or center of the workplace.
4. Definition of the traceable objective by selecting reflective markers.
5. Determination of the center of the traceable objective to follow it.



**Fig. 12.** OptiHub and cameras optitrack.



**Fig. 13.** Cameras Flex-3 calibration.

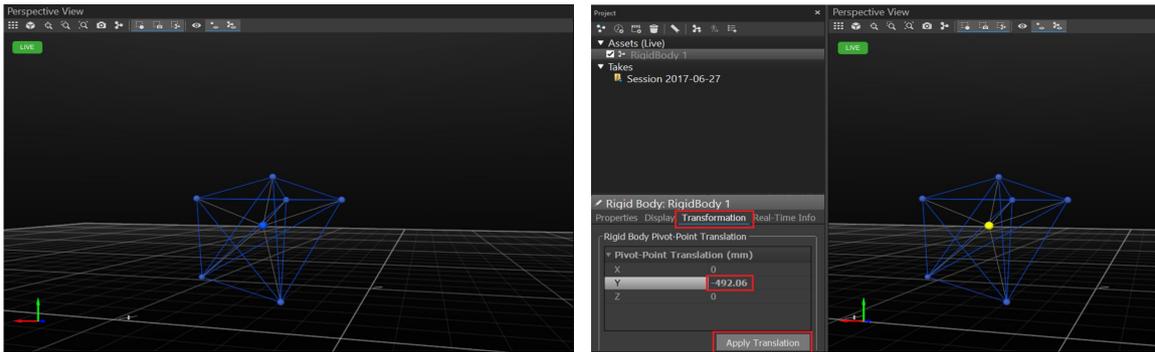


Fig. 14. Definition of the traceable objective.

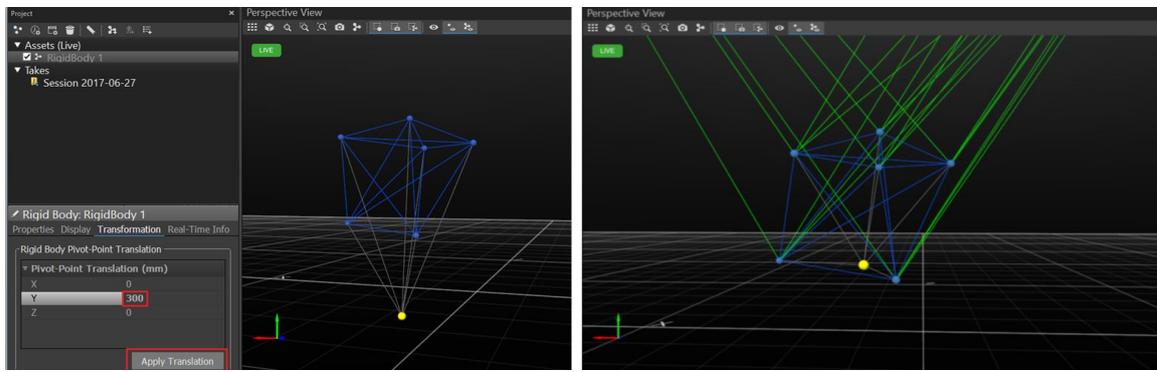


Fig. 15. Created the rigid body.

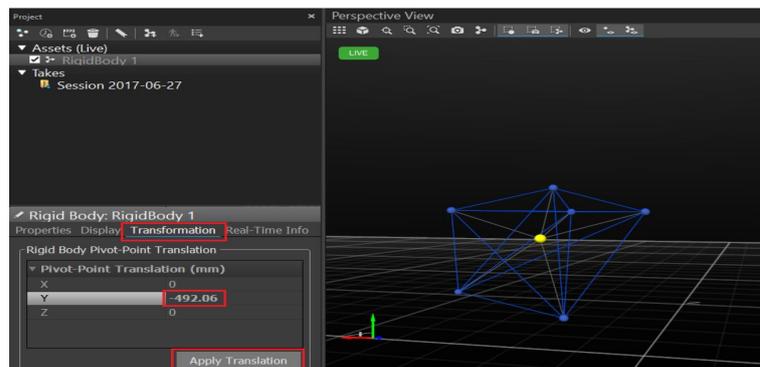
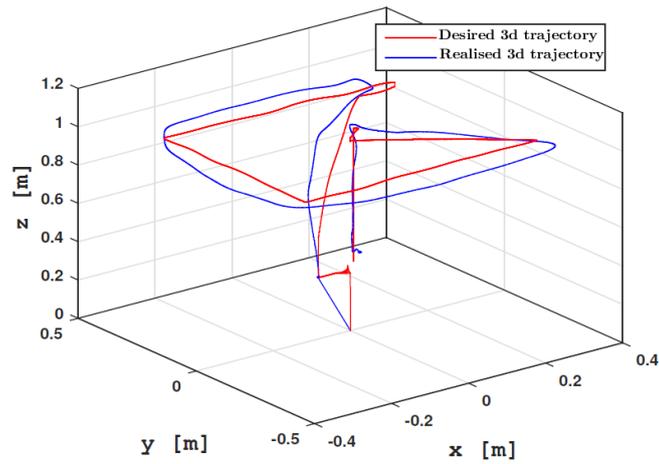


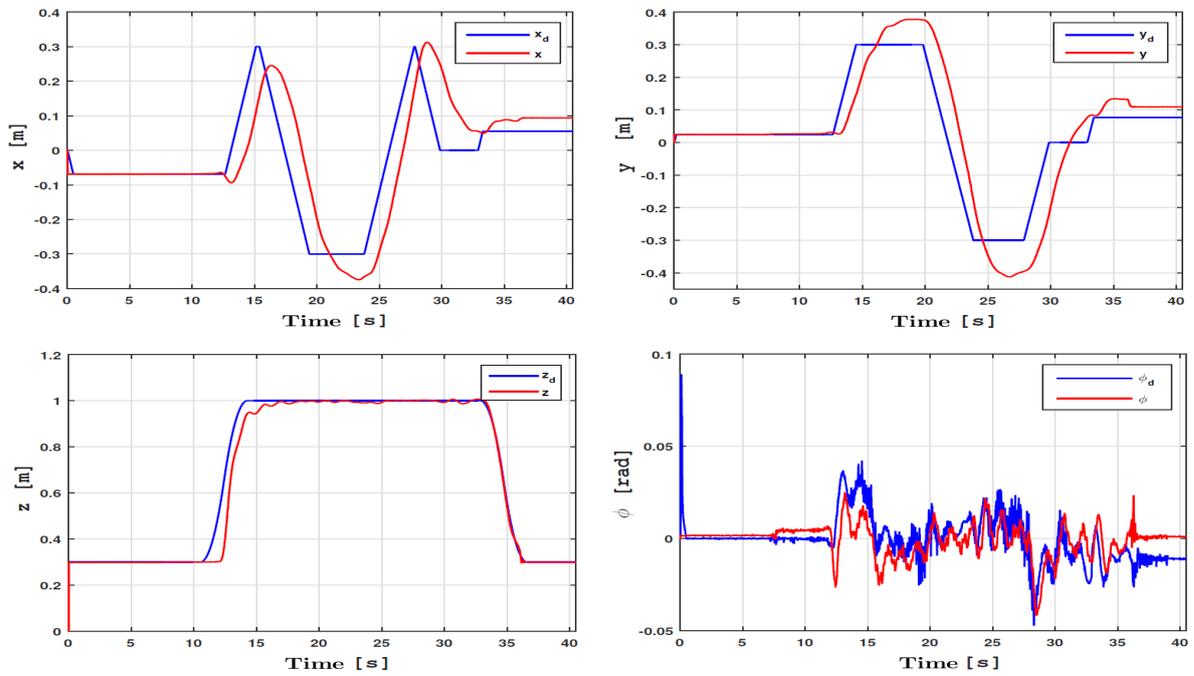
Fig. 16. Change of the geometric center of the body.

## 5.2. Flight Scenario

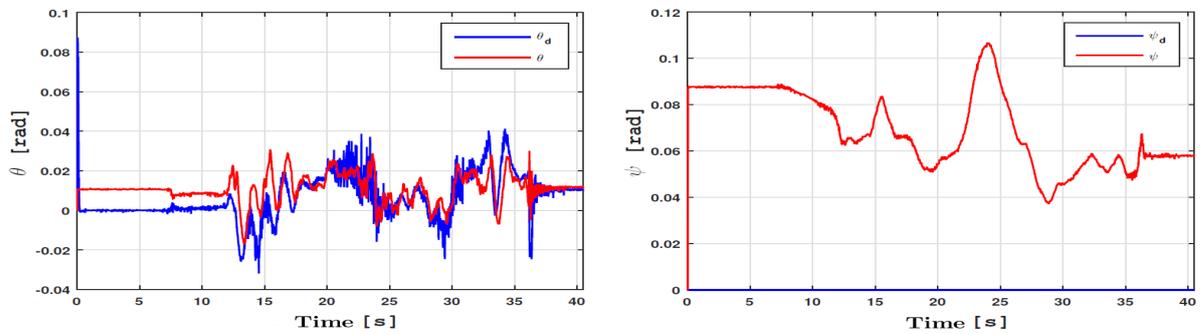
The QBall 2+ is controlled to follow the desired points in a frame of  $-0.3m$  to  $0.3m$ . After reaching a safety height of 1 meter, the quadrotor moves in the plane (X-Y) passing through the desired points (way points) as shown in Fig. 17. The experiment results (see Fig. 17, Fig. 18, Fig. 19 and Fig. 20) have shown similarities with those obtained by simulation (see Fig. 4, Fig. 5 and Fig. 7). Effectively, the difference between the obtained results (simulation and experiment) is mainly due to the neglected parameters of the model used in simulation.



**Fig. 17.** Evolution of 3D trajectory for PID controller in experimental tests.



**Fig. 18.** Evolution of positions and roll angle in experimental tests.



**Fig. 19.** Evolution of pitch and yaw angles in experimental tests.

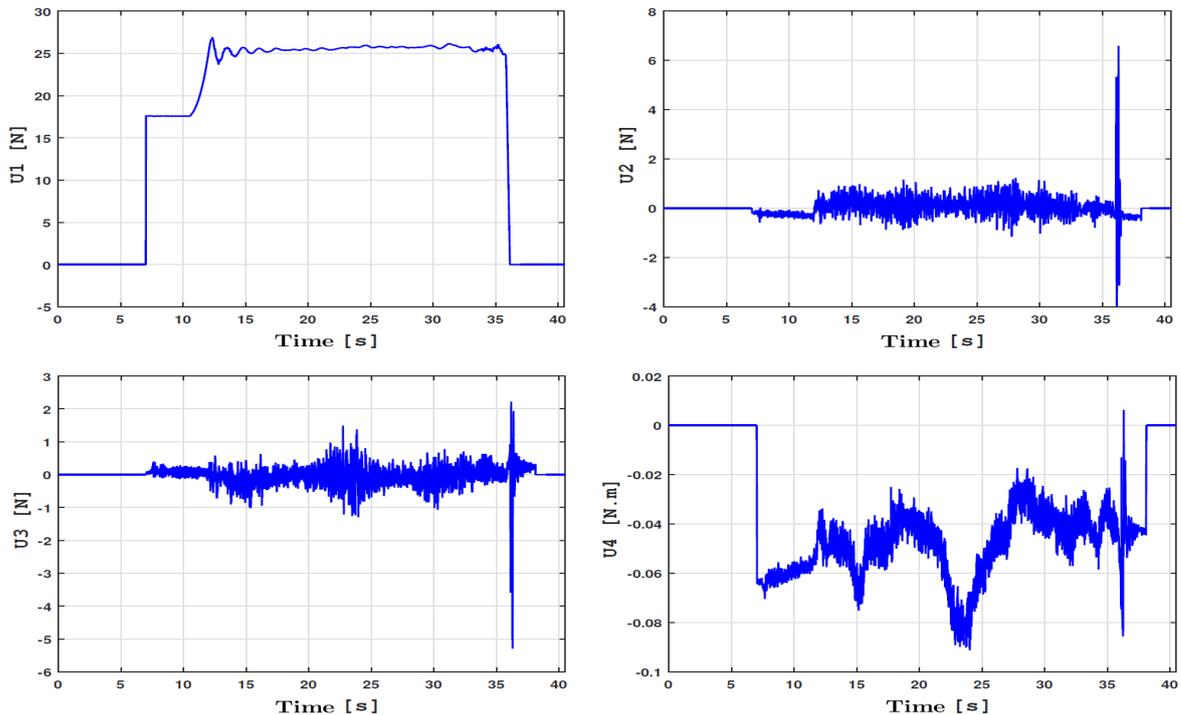


Fig. 20. Evolution of control signals in experimental tests.

## 6. Conclusion and Future Works

Within this article, a dynamic model of the QBall 2+ quadrotor has been developed. In addition, its linear model has been exploited to obtain the appropriate gains of the PID controller. Furthermore, to estimate the uncertain parameters of the system, a nonlinear SMC based on SMO has been developed. The latter has proven its efficiency and robustness against these parameters. Finally, to validate the obtained simulation results, the PID controller has been implemented in the flight control of the QBall 2+. The obtained results of the flight tests have shown a similitude to those obtained by simulation. In future works, the designed observer will be implemented and tested in the real system. In addition, the fault tolerant control problem will also be investigated.

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